Name

Class

GCSE Mathematics Specification

Paper 1 Higher Tier

For **AQA**

Churchill Paper 1A

Materials

For this paper you must have:

mathematical instruments

You must not use a calculator

Instructions

- Use black ink or black ball-point pen.
- Draw diagrams in pencil.
- Write your name and class in the box at the top of the page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- In all calculations, show clearly how you work out your answer.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.



Written by Shaun Armstrong

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Η

1 hour 30 minutes

			Ans	swer all (questio	ns in tł	ne spac	es pro	vided.	
1	What is the	e mediar	n of thi	s set of	data?					
	2 Circle your	4 answer	4	4 6	õ 7	8	8	9		
		4		5			6		6.5	[1 mark]
2	Asad is pa How much	id £10.6 does A	0 per l sad ge	nour. et paid fo	or 3 ¹ / ₂ h	iours w	vork?			
	Circle your	answer			2					[1 mark]
		£31.80		£35	.30		£36.80		£37.10	
3	What is the	e next te	erm in t	his geor	netric p	orogres	sion?			
	Circle your	2 answer	2 6	18	54					[1 mark]
		72		162			166		2916	
4	Work out	$\frac{3}{10} \div$	<u>1</u> 2							
	Circle your	answer								[1 mark]
		<u>3</u> 20		- -	<u>3</u> 5		<u>5</u> 6		1	

	5 Toby makes bracelets by putting 8 beads, 4 spacers and a heart charm on a silver chain. He buys the separate items in bulk at the following prices:					
		20 silver chains	£180			
		500 beads	£750	(())		
		100 spacers	£90			
		30 heart charms	£120	unger		
5	(a)	Work out the cost of the n	naterials for one bracelet.	[3 marks]		
			Answer £			
	At a	market one day, Toby sells	15 bracelets for £39.90 eac	ch.		
5	At a (b)	market one day, Toby sells How much profit does he	15 bracelets for £39.90 eac make at the market?	ch. [2 marks]		
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5	At a (b)	market one day, Toby sells How much profit does he	Answer £	ch. [2 marks]		
5	At a (b)	market one day, Toby sells How much profit does he	Answer £	ch. [2 marks]		



The angles in triangle *ABC* are given in degrees.

Prove that AB = AC.

6

[4 marks]

7	A m	nodel of bicycle is available in 5 frame sizes.	
	For The	each frame size there are 7 possible colours. are are 3 sets of gears that can be fitted on the smallest 2 frame sizes and 6 sets	that can
_			
7	(a)	Noah is buying the largest frame size.	
		In how many different ways can he choose the colour and gears for his bike?	[1 mark]
		Answer	
7	(b)	Here is part of a leaflet about this model of bike.	
		Available in combinations of frame size, colour and gears	
		What number is missing from the leaflet?	2 marks]
		Answer	

8 A bag contains only red beads and blue beads.

Faria picks out a bead at random, notes its colour and puts the bead back. Faria does this 10 times and gets a red bead 7 times.

Faria says "There are more red beads than blue beads in the bag."

8 (a) Comment on Faria's statement.

[1 mark]

Rosa, Shamila and Tess each do the same experiment as Faria. Here are all the results.

	Number of times a red bead is picked	Number of times a blue bead is picked
Faria	7	3
Rosa	6	4
Shamila	8	2
Tess	6	4

Faria is going to pick out another bead and put it back in the bag.

8 (b) Using the results in the table, work out the best estimate for the probability that she picks out a red bead.

Answer

[2 marks]

	In ar Faria She	nother bag contai a is going to pick says	ning beads, 60% out two beads at i	of the beads are g random from the b	reen. bag.	
		"The probability	of both beads be	ing green is $\frac{1}{3}$ as	you work out $\frac{0}{10} \times \frac{3}{9}$	
8	(c)	Is Faria correct	?			
		Explain your an	swer.			[2 marks]
9	Give	en that				
		<i>p</i> = 4 <i>q</i>	– 7			
	circl	e the expression	that gives <i>q</i> in terr	ms of <i>p</i> .		[1 mark]
		n + 7		n	7	[1 mark]
		$\frac{p+r}{4}$	7 <i>p</i> – 4	$\frac{p}{4} + 7$	$p + \frac{7}{4}$	

10	Jere	my, Kira and Liz are maths teachers.	
	Jere Kira Liz c	my can mark 12 homeworks in an hour. can mark 30 homeworks in 2 hours. an mark 1 homework every 6 minutes.	
10	(a)	Show that Kira is the quickest of the three teachers at marking homework.	[2 marks]
	One	night Jeremy and Kira work together to mark 36 homeworks	
	They	both start at 4.30 pm and work until all the homeworks are marked.	
10	(b)	At what time do Jeremy and Kira finish marking?	[3 marks]
		Answer	

11	The number of emails	eanne sent this v	veek is 20% more th	nan last week.	
	Work out how many en	nails Leanne sent	last week.		[2 marks]
		Answer			
12	<i>P</i> is a point on a circle, The straight line <i>XY</i> is	centre O. a tangent to the ci	rcle at the point <i>P</i> .		
	x	P 38 0	P ⁰ Y	Not drawn accurately	
	What is the value of <i>a</i> ? Circle your answer.				14
	38	52	58	62	[1 mark]

13	The ratio of men to women at a concert is 2:3	

There are 600 people at the concert.

How many men are there at the concert?

Circle your answer.

[1 mark]

120 200 240 250

14 A company selling clothes online decided to check the productivity of its workers. The table summarises the number of orders, *N*, packaged by 120 employees on one afternoon.

Number of orders (N)	Frequency
40 < <i>N</i> ≤ 45	4
$45 < N \le 50$	17
50 < <i>N</i> ≤ 55	33
$55 < N \le 60$	25
$60 < N \le 65$	20
$65 < N \le 70$	14
70 < <i>N</i> ≤ 75	7

14 (a) Complete this cumulative frequency table.

Number of orders (<i>N</i>)	Cumulative Frequency
$40 < N \leq 45$	4
$40 < N \leq 50$	
$40 < N \le 55$	
$40 < N \leq 60$	
$40 < N \le 65$	
$40 < N \le 70$	
$40 < N \le 75$	

[2 marks]





The diagram shows a square and two circles. The inner circle is the largest one that can be drawn inside the square. The outer circle is the smallest one that can be drawn with the square inside it.

Prove that the shaded area between the two circles is the same as the area enclosed by the inner circle.

[4 marks]



16	Henrik and R	ob both work r	part-time in a shop.
10	TICHIN AND IN		part-unite in a shop

In a normal week the ratio of what Henrik earns to what Rob earns is 3:2

In the week before Christmas they each receive a ± 20 bonus. The bonus means that the ratio of what Henrik earns to what Rob earns becomes 4:3

How much does Henrik earn in the week before Christmas?

[4 marks]

Answer £



17	(c)	Work out the total o	[3 marks]			
			Answer			m
18	Worl	k out $4^{-2} \times 8^{3}$				
	Circl	e your answer.				[1 mark]
		$\frac{1}{2}$	32	64	128	
		2				

	$5y - (2 \times 10^6) = 4 \times 10^7$	
	Give your answer in standard form.	[3 marks
	Answer	-
0	David says	
	"The value of \sqrt{x} is greater than the value of $\sqrt[4]{x}$ for all positive values of	of <i>x</i> ."
	"The value of \sqrt{x} is greater than the value of $\sqrt[4]{x}$ for all positive values of Decide whether or not David is correct. Show working to justify your answer.	of <i>x</i> ."
	"The value of \sqrt{x} is greater than the value of $\sqrt[4]{x}$ for all positive values of Decide whether or not David is correct. Show working to justify your answer.	of x." [2 marks
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	"The value of √x is greater than the value of ∜x for all positive values of Decide whether or not David is correct. Show working to justify your answer.	of x."

21	The functions f and g are defined as follows.			
		f(x) = 3x - 1	$g(x) = \frac{x+3}{2}$	
	Eval	uate		
21	(a)	fg(5),		[2 marks]
			Answer	
21	(b)	g ^{−1} (−2).		
				[2 marks]
			Answer	

22 (a) Complete this table of exact values.

sin 0°	sin 30°	sin 45°	sin 60°	sin 90°
0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$		

[1 mark]

22 (b) Triangles ABC and PQR are shown below.



By working out the exact area of each triangle, find out which one has the larger area.

[3 marks]



24		A X	Not drawn accurately	
	C		c	
	Qua	drilateral OABC is shown above.		
	ŌĂ	= 4 p , \overrightarrow{OB} = 3 p + 3 q and \overrightarrow{OC} = 6 q .		
	X is Y is	the midpoint of OA. the point on OC such that YC = 2OY.		
24	(a)	Express $\overline{X}\overline{Y}$ in terms of p and q .		[2 marks]
		Answer		_
24	(b)	Show that <i>BC</i> is parallel to <i>XY</i> .		[2 marks]

25	(a)	Express $x^{2} + 4x - 3$ in the form $(x + p)^{2} + q$.	[2 marks]
		Answer	
25	(b)	Hence, solve the equation	
		$x^2 + 4x - 3 = 0$	[1 mark]
		Answer	
25	(c)	The solutions of the equation $y^2 + ay + b = 0$ are	
		$y = 1 + \sqrt{2}$ and $y = 1 - \sqrt{2}$	
		Find the values of the integers <i>a</i> and <i>b</i> .	[3 marks]
		a =	
		b =	
		END OF QUESTIONS	